

For an excellent grade you have to get minimum of 9 questions accepted of each set, for a 'good' - at least 7, and for 'passed' - 5 questions.

## Finite group representation

**Problem 4.1:** Find transposition representation of  $S_3$ .

**Problem 4.2:** Decompose transposition representation of  $S_3$  to direct sum of representations.

**Problem 4.3:** Let  $G$  be a cyclic group. Find all irreducible representations of  $G$ .

**Problem 4.4:** Show that if representation  $\phi$  is one-dimensional, then commutant  $[G, G]$  lies in the kernel of representation.

**Problem 4.5:** Construct any representation of  $S_4$ . Which symmetry it describes? Find its character.

**Problem 4.6:** Consider any other  $S_4$  symmetry. Find the character of the corresponding representation.

**Problem 4.7:** Find all 1-dimensional representations of  $S_n$

**Problem 4.8:** Write tables of characters for  $S_4$

**Problem 4.9:** Show that for finite group  $G$  the amount of irreducible non-equivalent by pairs complex representations is equal to the amount of conjugacy classes.